# The Determinants of Teachers' Occupational 

## Choice*

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October 27, 2019


#### Abstract

We examine the appropriate fit of a dynamic optimization model with an application to teacher earning structure. To do so, we adjust the specification of the model by varying the unobserved heterogeneity in individuals' preferences and earnings. We find that even a model with no unobserved heterogeneity fits well within sample. Testing formally selects models with substantial unobserved heterogeneity, suggesting that relying on in-sample fit is problematic. In the application to teacher earnings, we show that a reform that adjusts teacher compensation to mimic the return to skills and riskiness of the non-teaching sector would be expensive and challenging; overall compensation in teaching would increase, but the majority of current teachers would be made worse off. Importantly, these conclusions are sensitive to the degree of heterogeneity allowed in the model.


Keywords: occupation choice, structural dynamic model, out-of sample fit, policy experiments

[^0]
## 1 Introduction

We make two contributions. On the methods side, we show that standard tests of insample fit can lead us to accept models with inadequate allowance for heterogeneity. On the substantive side, we examine the feasibility of a policy that makes the earnings structure for teachers more closely resemble that outside of teaching.

One of the strengths of structural models is that they allow us to consider experiments that lie outside the data. However, the validity of these experiments relies on the correct specification of the model. To understand the effect of a reform in the earnings structure of teachers, we estimate a dynamic model of occupation choice in which individuals decide each year whether to work as a teacher, in some other occupation, or not to be employed. The decision is dynamic because there are sector-specific returns to experience and because there is a cost of moving among the sectors. ${ }^{1}$

Our model is closest in both format and spirit to (Stinebrickner, 2001a) and particularly (Stinebrickner, 2001b). There are, however, some important differences in our treatment of uncertainty and of variation in the importance of earnings in the utility function. In addition, unlike him, we do not limit our sample to individuals who obtain their teaching qualification early on but consider all college graduates. The policy changes of interest to us may affect the decision to obtain a teaching qualification. We are also able to follow individuals much later into their careers which allows us to consider exit from and reentry into teaching. Moreover, we estimate the model with different degrees of unobserved heterogeneity (allowing for one "type" and up to nine "types" of individuals that differ in their preferences and abilities).

To choose the 'correct' amount of heterogeneity we use both the Bayesian Infor-

[^1]mation Criterion (BIC) and cross-validation using different numbers of unobserved types. The BIC favors using seven types out of the nine models compared, while the cross-validation weakly favors nine types while strongly favoring seven over fewer than seven types. In choosing the right amount of heterogeneity, we face two risks. If we allow for insufficient heterogeneity, the model is misspecified. If we allow for excess heterogeneity, although the estimates remain consistent, our counterfactual estimates may suffer from overfitting the original model.

Strikingly even the model with no unobserved heterogeneity appears to fit the data well in sample. Moreover, all models predict average teacher and non-teacher earnings well in sample. But when we test their out-of sample accuracy on our test samples, we need at least five types to fit average teacher and non-teacher earnings. And while, again, all models fit the characteristics of workers changing jobs well in sample, none does well out of sample.

The need for a large number of types does not arise in any obvious way from the peculiarities of our model. Our model requires little, if any, unobserved heterogeneity to fit well visually withing sample. It is only because we rely on formal mechanisms for model selection that we 'need' so much unobserved heterogeneity.

We use the model estimated to assess the feasibility of a policy that would make teachers earnings' structure closer to that outside of teaching. Teacher salaries are typically based on salary scales that depend only on education, experience and seniority and not on measures of quality of achievement. Not surprisingly, among college graduates, teachers have both low AFQT and high risk aversion. However, we know that, at least in other settings (e.g., Lazear, 2000), tying compensation more closely to performance can both increase the productivity of a fixed set of individuals and attract more productive individuals. Hoxby and Leigh (2004) provide support for
this hypothesis in teaching (see also Bacolod, 2007). ${ }^{2}$ As well, using a simulation Rothstein (2015) suggests that salary increases help attract and retain high ability teachers. Consequently, there is considerable interest in performance pay for teachers (see for example, the National Research Council report, Hout and Elliott, 2011).

We do not examine performance pay, per se, but we ask how the composition of the teaching profession would change if education and ability were compensated in the same way as in the general labor market for college graduates, presumably making teaching a similarly risky occupation. Like much of this literature, we look at the effect on general ability as measured by test scores and/or potential earnings outside teaching since we do not have a measure of teacher effectiveness. Our estimates of a strong correlation between potential earnings in teaching and non-teaching support our assumption that ability within and outside teaching are correlated, albeit imperfectly.

We find that rewarding measured and unmeasured ability within teaching as they are outside teaching leads to a shift of the more skilled types to teaching and slightly raises the average AFQT of teachers. But even this conclusion ignores the difficulty of effecting a transition. Reform requires transitioning to a compensation system that rewards characteristics differently from the current system and increases risk for a population that is risk averse relative to other college graduates. The reform we study would make a substantial proportion of experienced teachers worse off. Reforms are therefore likely to be disruptive in the short run, regardless of whether they are beneficial in the long run. ${ }^{3}$

Importantly, our results suggest strong caution about drawing policy conclusions

[^2]from models that fit well visually within sample. Our conclusions turn out to be very sensitive to the extent to which we allow for unobserved individual heterogeneity. With no formal tests for model selection, one could easily conclude that allowing for two or three unobserved types is adequate. But the point estimates of the simulation results are quite different if we allow for four types and dramatically different if we allow for five or six types. With seven or more types, our point estimates from the simulation results are again quite different from those with five or six.

## 2 Data and Some Empirical Regularities

We reverse the usual order of presentation and discuss the data before the model because certain regularities will influence how we develop the model.

We use the National Longitudinal Survey of Youth 1979 (NLSY79). Since the NLSY79 is well-known to labor economists, we skip a general description of the survey. We restrict the sample to college graduates and drop observations for years in which individuals report being self-employed, in the military or working fewer than 35 hours a week. Finally, we drop individuals interviewed fewer than four times. Table 1 shows summary statistics for the 1,077 individuals in our sample, divided into three categories: (1) teachers, (2) non-teachers and (3) not working. Note that an individual might be in all three categories over the course of the panel.

Compensation over the Lifecycle: Table 1 shows that teachers, on average, earn less than other college graduates. As shown in Figure 1(a), teachers' and nonteachers' have similar earnings when 22 years old, but a gap emerges as they age. By the time they are 55 years old, non-teachers earn almost 56 thousand dollars ${ }^{4}$ more than teachers do. This pattern does not merely reflect the changing composition

[^3]of the various groups over the lifecycle. Controlling for individual fixed effects or restricting the estimates to individuals who are only teachers or only non-teachers does not substantially change the pattern.

Risk and Uncertainty: The standard deviation of earnings is initially small and similar for teachers and non-teachers, but as age increases, the standard deviation remains modest for teachers and grows dramatically for non-teachers (see Figure $1(\mathrm{~b}))$. Since the residual could reflect factors known to the individual but not the econometrician, this does not necessarily imply that teaching is less risky than other occupations, but it is suggestive. And, in fact, if we regress log earnings on schooling, experience, year fixed effects and individual fixed effects, residual earnings variation is higher and grows faster among non-teachers.

Risk aversion: Therefore, we would expect risk-averse individuals to sort into teaching. We construct a risk-aversion parameter using three questions that were asked in each of four years: ${ }^{5}$ (1) Would you take a job that could double your income or cut it by $1 / 2$ with a $50-50$ chance?, (2) Would you take a job that could double your income or cut it by $1 / 3$ with a 50-50 chance?, and (3) Would you take a job that could double your income or cut it by $1 / 5$ with a $50-50$ chance? Using the responses to these questions we construct a risk aversion parameter. We assign a " 1 " to individuals who responded yes to the three questions, then a " 2 " to individuals who responded no to question one but yes to the other two, then we assign a " 3 " to individuals who responded no to questions one and two but yes to the last one, and finally we give a " 4 " to the most risk averse individuals who responded no to all questions. Because the same questions were asked in several years, the risk aversion parameter for a given individual may change. To have a measure of risk aversion for every year we use the most recent risk aversion parameter available for each individual.

[^4]As shown in Table 1, teachers are more risk averse than individuals working in other occupations.

Measured skills: Since teachers are rewarded for their education, we would not be surprised if they had higher average levels of education than workers in other occupations even among college graduates. This is confirmed in Table 1. In fact, in 2000 (when our sample is between 35 and 43 years old) $72 \%$ of teachers had graduate studies ${ }^{6}$ compared with only $43 \%$ of non-teachers and $17 \%$ of individuals out of the labor force.

However, Table 1 shows that teachers generally have less skill as measured by the AFQT, measured when the sample was 15-23 years old. The mean AFQT percentile, adjusted for the age at which the individual took that test, for teachers in our sample is 67 while the mean percentile for non-teachers is 75 . This "observable ability" measure is lower for teachers of all age groups (not shown).

Occupational mobility: Table 2 shows that mobility between teaching and nonteaching is modest. Fully $93.3 \%$ of individuals who are teachers in one year continue as teachers the following year, while only $5.2 \%$ move to a non-teaching occupation even though non-teachers account for $86 \%$ of the person-years in our sample. Mobility from non-teaching to teaching is rarer. As can be seen from the second row of the table, only $0.8 \%$ of non-teachers transition to teachers in an average year even though teachers account for $11 \%$ of the person-years in our sample.

[^5]
## 3 Model and estimation

### 3.1 Occupation choice

The one-period utility function depends on the decision made, on expected earnings ${ }^{7}$ and on the nonpecuniary characteristics of the occupations. We do not model these characteristics since we are modeling the choice of teaching versus non-teaching rather than the choice among admittedly heterogeneous jobs within these broader occupations. If all individuals valued the nonpecuniary components equally, we could capture their value by adding occupation-specific constants to the utility function. The teaching constant would capture the utility, net of earnings and risk, of working as a teacher relative to not working and similarly for the non-teaching constant. The difference between the coefficients would capture the utility of teaching relative to non-teaching.

Of course, people with different characteristics may value the nonpecuniary characteristics in systematically different ways. To capture these differences, we include additional sociodemographic controls in the utility function. Since we specify different utility functions for teaching and non-teaching except for the effect of earnings, these sociodemographic controls are implicitly interacted with occupation.

Finally, we allow for the possibility that it is costly to transition between states. It may, for example, take time to adjust to the different nature of the working environment in teaching or non-teaching.

Consequently, utility in each state $d$ depends on the state variables $s_{i t}=\left\{\bar{Z}_{i t}^{d}, \xi_{i t}^{d}\right\}$

[^6]as given by
\[

$$
\begin{align*}
U_{i t}^{d}\left(s_{i t}\right) & =u\left(d, \bar{Z}_{i t}^{d}\right)+\xi_{i t}^{d}  \tag{1}\\
& =\theta_{u 1} E\left[w_{i t}^{d}\right]+\theta_{u 2}\left(E\left[w_{i t}^{d}\right]\right)^{2}+\theta_{u 3}^{d} z_{i t}+\theta_{u 4}^{d}\left(1-d_{i, t-1}\right)+\theta_{u 5}^{d} o_{i, t-1}+\xi_{i t}^{d} \tag{2}
\end{align*}
$$
\]

where $\bar{Z}_{i t}^{d}:=\left\{E\left[w_{i t}^{d}\right], z_{i t}, d_{i, t-1}, o_{i, t-1}\right\}$ represents the observed state variables. $E\left[w_{i t}^{d}\right]$ is expected earnings and $z_{i t}$ includes individuals' characteristics such as gender, marital status, risk aversion, age, AFQT percentile, schooling ${ }^{8}$ and whether the individual has children. $d_{i, t-1}$ is a dummy variable equal to one if individual $i$ chose occupation $d$ in period $t-1$ and zero otherwise. $o_{i, t-1}$ is also a dummy variable, equal to one if individual $i$ chose not to work in period $t-1$ and zero otherwise. Thus, $\theta_{u 4}^{d}$ is the cost of transitioning into occupation $d$ from the other occupation and $\theta_{u 5}^{d}$ is the cost of transitioning into occupation $d$ from non-employment. We normalize the utility associated with non-employment to be 0 . We also set the cost of transitioning to nonemployment at 0 . Risk aversion is only measured in four surveys. We hold it fixed between these and assume that individuals know their future risk aversion.

The individual's unobserved preferences for each occupation (taste shocks) are given by the $\xi_{i t}^{d}$. We assume the $\xi_{i t}^{d}$ 's are taken from an extreme value type I distribution and temporarily assume that the errors are serially uncorrelated. Later, we will address serial correlation by allowing for multiple types.

We model the occupation choice process as consisting of $(T-\hat{t})$ periods, where $T$ is the retirement date, which we will generally impose to be age 60 , and $\hat{t}$ is the first year the individual enters the workforce. Each period, individuals can choose among teaching, other jobs (non-teaching) and non-employment. If they decide to work, their earnings depend on their occupation choice.

[^7]Individuals are forward-looking. When choosing an occupation in period $t$, they take into account not only the one-period utilities associated with the choices but also their effect on sector-specific experience and therefore on future earnings. In addition, they may face a switching cost.

From entry into the workforce until retirement $(T)$, individuals weigh the consequences of their decisions for future utility. A full solution of the dynamic programming problem consists of finding $E\left[\max \left(V_{t}^{1}\left(s_{i t}\right), V_{t}^{2}\left(s_{i t}\right), V_{t}^{3}\left(s_{i t}\right)\right)\right]$ at all values of $z_{i t}$, $E\left(w_{i t}^{d}\right), d_{i, t-1}$ and $o_{i, t-1}$ for all $t$, where the choice-specific value function is:

$$
V_{t}^{d}\left(s_{i t}\right)= \begin{cases}U_{i t}^{d}+\delta E\left[V_{t+1}\left(s_{i, t+1}\right) \mid s_{i t}, d_{i t}=d\right] & \text { if } t<T  \tag{3}\\ U_{i t}^{d} & \text { if } t=T\end{cases}
$$

The choice-specific value function $V_{t}^{d}\left(s_{i t}\right)$ can be decomposed as $v_{i t}^{d}+\xi_{i t}^{d}$, where $v_{i t}^{d}$ is the expected choice-specific value function that has a closed form solution. We set the discount factor $\delta$ equal to $0.95 .{ }^{9}$ Given the extreme value assumption for the distribution of taste shocks, the probability of an individual choosing occupation $d$ in period $t$ takes a logit form:

$$
\begin{equation*}
P\left(d_{i t}=d \mid \bar{Z}_{i t}, \theta_{u}\right)=\frac{\exp \left(v_{i t}^{d}\right)}{\sum_{d} \exp \left(v_{i t}^{d}\right)} \tag{4}
\end{equation*}
$$

where the sums are taken over the three possible options available to the individual. Since we have a finite time horizon, and taste shocks are distributed as an extreme value type I, expected value functions have a closed form analytical expression and can be calculated by backward induction. For a more detailed discussion on estimation of discrete choice dynamic programming models see Aguirregabiria and Mira (2010)

[^8]and Arcidiacono and Ellickson (2011).

### 3.2 Earnings

Earnings depend on the occupation chosen and are a function of a time trend which also captures linear age effects, individual characteristics, and experience in the teaching and non-teaching sectors. Thus log earnings for a given decision $d=\{$ teacher, non-teacher $\}$ in year $t$ for individual $i$ are given by:

$$
\begin{align*}
\log \left(w_{i t}^{d}\right) & =\theta_{w}^{d} \bar{X}_{i t}^{d}+\epsilon_{i t}^{d}  \tag{5}\\
& =\theta_{w 1}^{d} f(\text { trend })+\theta_{w 2}^{d} x_{i}+\theta_{w 3}^{d} g_{i t}^{d}+\theta_{w 4}^{d} f\left(\exp T_{i t}\right)+\ldots \\
& \theta_{w 5}^{d} f\left(\exp N_{i t}\right)+\epsilon_{i t}^{d} \tag{6}
\end{align*}
$$

where $x_{i}$ includes gender, marital status, race, AFQT score and whether the individual has children.

Schooling, $g_{i t}$, is occupation specific. For any observed decision, schooling is just the number of years of education that individual $i$ has, but for the alternative choices we assume individuals would have at least the same schooling as the contemporaneous average individual in that occupation, that is $g=\max \{$ actual education, average education in occupation $\}$. For instance, if individual $i$ decides to be a non-teacher in period $t$ and has sixteen years of schooling then $g_{i t}$ for her non-teaching log earnings equation is sixteen. However, if the average schooling of teachers of her age is higher, say eighteen years, then schooling for individual $i$ at time $t$ for her teaching log earnings equation is eighteen. This implies that individual $i$ would get more schooling if she decided to be a teacher. Since we are not modeling schooling decisions and education is explicitly rewarded in teacher
compensation contracts, allowing for education to be higher for off-path decisions is an important feature of a teacher-occupation-choice model.

The occupation-specific experience terms, experience as a teacher $\left(\exp T_{i t}\right)$ and experience as a non-teacher $\left(\exp N_{i t}\right)$, evolve depending on the individual's choices. $f($. is a quadratic function. Finally, the shocks (the $\epsilon_{i t}^{d}$ 's) are unknown to the individual at the time of the decision and are assumed to be normally distributed with mean zero and variance $\sigma_{d}^{2}$. We want to capture the fact that the variance of earnings increases with age (or experience). This is particularly true for the non-teaching occupation. Therefore, we model the $\sigma_{d}$ 's as linear functions of age. For identification of the coefficient on earnings in the utility function it is crucial that an exclusion restriction exists, a variable appearing in the earnings equation and only affecting utility through earnings. We use the sector-specific experience terms as the exclusion restriction.

### 3.3 Heterogeneity, serial correlation and selection

So far, we have assumed that unobserved preferences and unobserved ability are both uncorrelated over time and uncorrelated with each other. Thus an intense unobservable preference for teaching in period $t$ would not be related with having an intense unobservable preference for teaching in period $t+1$. Similarly, there is no persistent unobserved ability which is known to the individual but not to the econometrician.

To address these concerns, suppose that there are $L$ types of people that differ in their preferences for each occupation and in their unobserved abilities. ${ }^{10}$ We allow the constant terms of the utility functions and log earnings equations, and the coefficients on the expected earnings terms in the utility functions to vary among types. Thus,

[^9]the utility and log earnings equations for type $l$ in occupation $d$ are:
\[

$$
\begin{align*}
U_{i t, l}^{d}\left(s_{i t}\right) & =\omega_{\mathbf{u}, \mathbf{l}}^{\mathbf{d}}+\theta_{\mathbf{u} 1, \mathbf{l}} \mathbf{E}\left[\mathbf{w}_{\mathbf{i t}, \mathbf{1}}^{\mathbf{d}}\right]+\theta_{\mathbf{u} 2, \mathbf{l}}\left(\mathbf{E}\left[\mathbf{w}_{\mathbf{i t}, \mathbf{l}}^{\mathbf{d}}\right]\right)^{2}+\theta_{u 3}^{d} z_{i t}+\ldots  \tag{7}\\
& \theta_{u 4}^{d}\left(1-d_{i, t-1}\right)+\theta_{u 5}^{d} o_{i, t-1}+\xi_{i t}^{d} \\
\log \left(w_{i t, l}^{d}\right) & =\omega_{\mathbf{w}, \mathbf{l}}^{\mathbf{d}}+\theta_{w}^{d} \bar{X}_{i t}^{d}+\epsilon_{i t}^{d} . \tag{8}
\end{align*}
$$
\]

Note that, for a given type, we restrict the coefficients on the expected earnings terms in the utility functions to be the same in teaching and non-teaching. Thus expected earnings in teaching and non-teaching occupations give type $l$ the same utility.

### 3.4 Estimation

We calculate the parameters using maximum likelihood. Without unobserved heterogeneity, the contribution of individual $i$ to the likelihood function is the product of the likelihood contribution of occupation decisions $P($.$) and the likelihood contribution$ of earnings $f_{w}($.$) :$

$$
\begin{equation*}
L_{i}(\theta) \equiv \prod_{t=1}^{T_{i}} P\left(d_{i t} \mid \bar{Z}_{i t}, \theta\right) f_{w}\left(\log \left(w_{i t}\right) \mid d_{i t}, \bar{X}_{i t}, \theta\right) \tag{9}
\end{equation*}
$$

To estimate the parameters when we include unobserved heterogeneity we use a mixture distribution, where $\pi_{l}$ is the proportion of the $l$ th type in the population. These proportions and the unobservable preferences and abilities are fixed over time, allowing us to control for serial correlation and selection. With unobserved hetero-
geneity the contribution of individual $i$ to the finite mixture of likelihoods is:

$$
\begin{equation*}
l_{i}(\theta, \Omega, \pi)=\log \left(\sum_{l=1}^{L} L_{i}\left(\theta_{l}, \omega_{l}\right) \cdot \pi_{l}\right) \tag{10}
\end{equation*}
$$

The set of structural parameters to estimate consists of 64 coefficients when there is no unobservable heterogeneity. For each additional type we include there are seven extra parameters. We estimate the model for one through nine types.

In the remainder of the paper, we primarily present the results without heterogeneity and with seven types since this is the number chosen using the BIC and since the results for seven, eight and nine types are similar.

## 4 Results

### 4.1 Choosing the number of types

The most obvious approach to model selection, a likelihood ratio (or similar) test, cannot be used because mixture models violate the requisite regularity conditions; some parameters are not identified under the null. An obvious alternative, Schwarz's Bayesian Information Criterion (BIC), ${ }^{11}$ tends to require a very large number of types, perhaps beyond what is numerically feasible in some contexts.

In our case, as shown in section 5 , visually our model fits the data well regardless of the number of types. We use two formal approaches to choose among the models. First, we calculate the BIC for each specification (see Table 3). The BIC continues to improve up to the seven-type model, but it is worse for the eight and nine-type models.

[^10]Second, we use a cross-validation approach. Our approach is based on the following logic. A properly specified maximum likelihood model minimizes out of sample prediction error (Hansen and Dumitrescu, 2016). Therefore, if we believe that one of our models is correctly specified, it should be the one that predicts best out of sample. Thus, we randomly divide our sample into two groups, consisting of $80 \%$ and $20 \%$ of individuals. We re-estimate the models using the larger sub-sample. Then, we use the new coefficients and the data from the other $20 \%$ of individuals and calculate the log-likelihoods for each of the nine models. We repeat this exercise twenty times and compare the out-of-sample log-likelihoods.

As with the BIC, this cross-validation approach suggests that we require a large number of unobservable types to address heterogeneity adequately. However, when comparing the seven and eight-type models the cross-validation approach suggests eight types is better. And when comparing the eight and nine-type models this approach also suggests that nine types is preferred. Still, there is some evidence that we are approaching the requisite number of types. In all twenty replications, four types does better out-of-sample than three types which in turn fits better than the model with two types which outperforms the model with one type. When we compare seven versus six, the model with more types predicts better out of sample in a clear majority of replications and averaged across replications, but there are replications that give the opposite result. The same is true when comparing six versus five and five versus four. However, when comparing eight and seven types, eight types does better out-of-sample in only 13 of the 20 sub-samples. If the two models fit equally well out of sample, and if the parameters were independent across draws (which they are not, because there is roughly 80 percent overlap), the probability of one model outperforming the other at least thirteen times would be 12 percent, suggesting little difference in the predictive power of the two models. Finally, the nine-type model
does better out-of-sample in only 11 of the 20 sub-samples when comparing it to the eight-type model. ${ }^{12}$

Consequently, we present the results of the model with seven types. For purposes of comparison, we also show the results without unobserved heterogeneity.

### 4.2 Estimates of the utility function

Table 4 displays estimates of the utility function parameters that are common to all types. Relative to non-employment, being risk averse increases the utility from teaching and reduces the utility from non-teaching. When we control for unobserved heterogeneity with the seven-type model, the point estimates for risk aversion in teachers' and non-teachers' utility functions still suggest that risk averse individuals tend to prefer teaching. In the absence of unobserved heterogeneity, among single individuals, conditional on the other controls, being male strongly increases the preference for nonemployment relative to both teaching and non-teaching with only a small difference between the two types of occupations. Their preference for non-teaching relative to teaching is more pronounced in the model with seven types.

Being married or with children seems to increase the preference for non-employment over teaching, and for teaching over other occupations for both females and males. These coefficients do not change substantially when controlling for unobserved heterogeneity.

Switching occupations and returning to employment is costly. Controlling for unobserved heterogeneity has very little effect on these coefficients. Using the estimates from the model with no unobserved heterogeneity, at average teacher earnings (of $\$ 51,100)$ switching from non-teacher to teacher is comparable to a decrease of $\$ 18,100$

[^11]in earnings that year and the cost of returning to employment is equivalent to $\$ 35,130$ in that year's earnings. At average non-teacher earnings (of $\$ 76,600$ ) switching occupation from teacher to non-teacher is comparable to a decrease of $\$ 21,800$ in earnings and the cost of returning to employment is equivalent to $\$ 39,300$ in that year's earnings.

Age, age squared, AFQT and schooling were also included in the estimation. The coefficients on AFQT are very similar for teachers and non-teachers. Whereas, more educated individuals prefer to work as a non-teacher.

The panels labeled Type x in Table 5 show the relation between types and utility. Each type except the first has an additional utility it receives relative to the first type from each of the occupations. These panels also show the full utility that each type receives from expected earnings (in 10,000's of 2012 dollars) and its square. With only one type, the marginal utility of earnings is increasing up to almost $\$ 200,000$, which covers $95 \%$ of our observations. When we allow for unobserved heterogeneity, all types except the first and fourth put more weight on earnings at low values than the single type does. The second type only values earnings up to about $\$ 118,000$ and the sixth only up to about $\$ 117,000$ while the other types have positive marginal utility of earnings up to $\$ 200,000$ or higher. ${ }^{13}$

### 4.3 Estimates of the log earnings equation

Table 6 shows the estimates of the log earnings equations. When we do not consider other forms of heterogeneity, the coefficient on AFQT percentile is lower for teachers. This is still true when we control for unobserved heterogeneity but the difference

[^12]between the coefficients on AFQT for teachers and non-teachers is smaller in the seven-type model than in the one-type model.

Not surprisingly returns to schooling are higher for teachers. As previously discussed, teachers with more years of education receive a higher salary. These coefficients are very similar when we increase the number of types. Also, for both occupation groups, among single and childless individuals, males' earnings are higher. The gender earnings gap for teachers increases and for non-teachers decreases with seven types, and is similar for both occupations in this specification.

Married individuals in the non-teaching occupation have higher earnings than nonmarried individuals. This difference is not statistically significant for teachers. Not surprisingly, females with children have lower earnings in both occupations than females with no children. However, earnings for males with children are not different for teachers and are even higher for non-teachers compared to males with no children. These coefficients are qualitatively similar in both models presented.

A key to identification of the coefficient on earnings in the utility function is to have a variable which is only in the log earnings regression. We use sector-specific experience as the exclusion restriction. The coefficients on experience basically do not change when including more types. Not surprisingly, teaching experience is particularly relevant for teachers. Teacher earnings increase with teaching experience and continue to do so beyond the range of experience found in our data. Small levels of teaching experience provide little benefit outside of teaching. However, our point estimates suggest that teachers with considerable experience benefit in other jobs. ${ }^{14}$ Overall, an extra year of teaching increases yearly earnings around $\$ 1,600$ for the average teacher, while it has an insignificant negative effect on yearly earnings for the

[^13]average non-teacher.
Experience in other occupations increases earnings for both teachers and nonteachers at a decreasing rate but throughout the relevant experience range nonteaching experience is more valuable outside of teaching.

Finally, the standard deviations are modeled as linear functions of age (i.e., $\sigma=$ $\left.\sigma_{A}+\sigma_{B} \cdot a g e\right)$. The estimates suggest that the variance of teachers' earnings is lower than the variance of non-teachers' earnings for all age groups.

The distribution of types across occupations (not shown) plays a modest role in the earnings gap between teachers and non-teachers. Most of the difference is due to how the types are rewarded. If the distribution of teachers by type were the distribution among non-teachers, their mean earnings would be roughly 13 percent higher. If the type distribution of non-teachers were that of teachers, their mean earnings would be 11 percent lower.

However, there is more variation in earnings across types outside of teaching than within teaching. The weighted standard deviation of the type effect in teaching is about 0.28 while it is about 0.36 outside of teaching. Types that are good at non-teaching also tend to have high earnings in teaching. The correlation is about 0.87 using the distribution of teachers across types and 0.72 using the non-teachers' distribution. In short, there is a strong positive correlation between the (to us) unmeasured skills that raise earnings within and outside teaching, ${ }^{15}$ but these skills are rewarded more generously outside teaching.

[^14]
## 5 Goodness of fit

It is common in structural papers to examine how well the model matches the data by displaying figures that compare predicted and observed averages. Some papers also calculate in-sample goodness-of-fit statistics. We show that, using these comparisons and statistics, all of our models seem to fit most data patterns well: occupation choices, earnings and characteristics of transitioning individuals. Then, we test the accuracy of out-of-sample predictions using the 80-20 cross-validation division explained in Section 4.1.

### 5.1 In-sample fit

We begin by describing the goodness of fit in-sample. Figures 2 and 3 show, for the one and seven-type models, the percentage of teachers and non-teachers by age. Visually both models fit well. As is evident from the figures, the fits of the models with one and seven types are essentially indistinguishable; this also applies to the models for which fit is not shown.

The seven-type model matches the average earnings of both teachers $(\$ 51,100)$ and non-teachers $(\$ 76,600)$ well in the sense that the predicted means lie within the 95 percent confidence interval of the estimated population means from the data ( $\$ 51,500$ and $\$ 75,400$ ). This is also true for the other models; the average earnings predicted lie within the confidence interval of the population means. ${ }^{16}$ Figure 4 depicts the log earnings by age for both groups, for the one and seven-type models. And, as is also evident, the fit of the model with one type is barely distinguishable from that with seven types. Using the seven-type model, the absolute deviations from the data for

[^15]different ages go from 0.0005 to 0.3984 for non-teachers and from 0.0005 to 0.3027 for teachers. These numbers are not very different for the other models. ${ }^{17}$ With Table 7, we see that the seven-type model replicates well transitions for non-teachers and not employed individuals. However, it over-predicts teachers' transitions into nonemployment and under-predicts teachers' transition to non-teaching occupations.

Finally, Table 8 shows the average characteristics of transitioning individuals. The model does a good job at matching observed averages in every cell. For every average, the model prediction is within the 95 percent confidence interval for the population average. The same applies for the other models estimated. An interesting pattern, well replicated by the models, is that individuals who are teachers in one year and continue as teachers the following year are very risk averse and have low cognitive skills. As for non-teachers who do not change occupation, both the observed and predicted averages show that they are not particularly risk averse and have an AFQT score slightly above average.

### 5.2 Cross-Validation

While, except for underestimating teachers transitions into other occupations, our models fit well, at least visually, within sample, a fairer test is their ability to predict out-of-sample in a cross-validation exercise. We take twenty random samples consisting of eighty percent of the individuals in our sample, reestimate the models and calculate how accurately we predict log earnings for that part of the sample that was not used in the estimation.

To assess how well our models predict earnings we calculate average earnings for

[^16]both groups, teachers and non-teachers, in every sub-sample and compare these averages with the out-of-sample predictions of our models. In the model with no unobservable heterogeneity, in fourteen of the twenty sub-samples for at least one of the two occupations, we reject the hypothesis that the predicted average is within the confidence interval of the observed population average of that group. For the two and three-type models, for seven of the twenty sub-samples we reject the hypothesis that predicted teachers' average earnings is within the confidence interval of the observed population average. For four types we reject this hypothesis in five of the twenty sub-samples, and for five types only in two of the twenty sub-samples. For every other model, with six, seven, eight or nine types, we reject this hypothesis in one or none of the twenty sub-samples. Thus we need at least five types to match average earnings out of sample.

Additionally, we analyze the deviations of predicted from observed earnings by age for the twenty sub-samples. We summarize this information in Figure 5. These are unconventional graphs; they show the root mean squared error (square root of the mean of deviations squared for the twenty sub-samples) from the one, two, five and seven-type models. There is little difference between the models shown and the seventype model; so we do not present results from all models. We also omit ages below 23 and above 53 years where deviations are larger due to a small number of observations. The "average deviations" depicted by age show a moderate decrease when comparing the one-type model and any of the models with unobservable heterogeneity.

Finally, we apply our approach to predicting the characteristics of transitioning individuals. In each case, we ask whether the prediction from the model matches the population mean allowing for the confidence interval around the estimate of the population mean but not the imprecision of the model estimate. We calculate the t-statistic for the hypothesis that the population average equals the model point
estimate. ${ }^{18}$ Table 9 shows the maximum t-statistic of the twenty draws for every cell for the seven-type model. Since we are performing multiple tests, we use Bonferroni's correction. If there is no correlation among the tests, the adjusted critical value at the 5 percent confidence level is 3.0233 . Since the tests are calculated with sub-samples drawn from the same master sample there should be some correlation among tests, so we can use 3.0233 as an upper bound and 1.96 as a lower bound. That is, we definitely reject the hypothesis that model and data averages are the same for cells with a t-statistic higher than 3.0233 , and we definitely cannot reject (at the 0.05 level) the hypothesis that model and data averages are statistically equal for cells with a t-statistic lower than 1.96. In the diagonal cells we definitely do not reject that predicted and observed averages are equivalent. On the other hand we can clearly reject the null for average AFQT and risk aversion of transitioning individuals. The results are almost identical for all models.

## 6 Simulation

While structural modeling enables us to perform counterfactual experiments, the credibility of such experiments relies on the model being a 'good enough' approximation of reality. When allowing for unobserved individual heterogeneity there are two risks. If we do not allow for sufficient heterogeneity, the model is misspecified. If we allow for excess heterogeneity, although the estimates remain consistent, our counterfactual estimates may suffer from overfitting the original model. Therefore, choosing the correct number of types is crucial, particularly if the results from simulations differ depending on the number of types.

In this section we show that the conclusions from our counterfactual experiment

[^17]are highly sensitive to the number of types. Using our nine specifications we simulate how teachers' characteristics, in particular AFQT and risk aversion, would vary if a different contract were offered. To assess the experiment's 'cost' we also calculate average earnings given the new environment. We are interested in analyzing the change in teacher composition keeping quantity constant, that is we want to keep average probabilities of being a teacher and a non-teacher unchanged. To achieve this we adjust the constant terms in the log earnings equations for each simulation.

To be clear, we are not simulating an ideal policy. Such a policy would require objective and/or subjective measures of teaching performance that are not available in our data for teachers, let alone non-teachers. Instead we rely on the positive relation between teaching and other skills to justify this experiment.

Our simulation considers a world in which salaries for teachers reward measured and unmeasured abilities in the same way as those of non-teachers. These changes imply an increase in the riskiness of the teaching occupation; there is much more variation in earnings across types outside of teaching than within teaching. To replicate this scenario we adjust several coefficients. First, we adjust teacher salaries so that they are as responsive to AFQT (our measure of "observable ability") and to schooling as those for non-teachers. Then, we replace the coefficients on the unobservable types in the log earnings equation for teachers with those from the non-teaching log earnings equation. Finally, we set the coefficient on risk aversion in the teacher utility equation equal to its value in the utility equation for non-teaching. We also adjust the constant term so that the utility from teaching for individuals with the lowest risk aversion measure is unaffected by the increased riskiness. ${ }^{19}$ We also raise teachers' earnings

[^18]variance by setting the $\sigma_{A}$ and $\sigma_{B}$ parameters equal to the parameters estimated in the non-teaching earnings equation. Due to the conversion from logs to levels, this increases expected earnings in the selection equations.

In summary, we are changing: the risk aversion parameter in the teacher utility equation and the AFQT, schooling, variance coefficients and types coefficients in the teacher log earnings equation. Finally, we adjust the constant terms from log earnings equations so that there is only a change in the composition of teachers and not in the quantity (or average probability).

Table 10 shows the average effect of the simulation using the nine models. The results shown are the predicted averages of the simulation minus the predicted averages of each model. Although we cannot compare whether the policy effects are statistically different among models, ${ }^{20}$ the point estimates differ dramatically depending on the number of types used, and the effects are not necessarily monotonic in the number of types.

Average AFQT basically remains unchanged using the three-type model and increases 0.36 standard deviations using the five-type model. The model with no unobserved heterogeneity and the eight-type model suggest the policy would increase average AFQT by 0.12 standard deviations.

Risk aversion, in turn, decreases by around 0.02 standard deviations with the one, two, and three-type models and around 0.05 standard deviations with the seven, eight and nine-type models. Yet, it decreases by more than 0.15 standard deviations with the five and six-type models.

The changes in age, gender and race are negligible for the one through four-type models and for the seven and eight-type models. With five types, the change in

[^19]average age is nontrivial. It is particularly striking that the share of males increases dramatically in the simulation using the five and six-type models. And we see a very notable decline in minority representation with five types and, to a lesser degree, with six types. Interestingly, the differences in the simulation results when using the seven, eight and nine-type models are rather small.

How much would such a change in policy cost? Here, again, the answer depends in important ways on the amount of heterogeneity we allow. The smallest 'cost' occurs when there are seven types, in which case average teaching salaries increase by $\$ 2,500$ per year or $5.0 \%$. The estimated costs are also modest with one type (5.4\%) and grow somewhat large with two (7.2\%), three (6.8\%), four (8.4\%), eight (7.5\%) or nine types (6.2\%). Our conclusions are strikingly different with five (18.4\%) or six types (20.3\%).

What accounts for these differences? Once we have more than one type, a large part of the change in the structure of earnings comes from the way that unobservable types are rewarded. As we include more types, the magnitude of the largest earnings gap for the type with the largest gap will tend to increase. This increases the value of switching from non-teaching to teaching for the group that benefits most from the change. Of course, this is not always the case, and the effect is partially offset by the tendency for the proportion of individuals in each type to fall. Thus the effect need not be monotonic. In our estimates and simulations with five and six types, we see a large shift of the most highly paid group into teaching.

Consistent with this explanation, the disruption required to effect such a policy is much greater in the simulations with five or six types. With one to three types we estimate that $12 \%-13 \%$ of teachers (weighted by teaching years) would leave teaching. When juxtaposed with an annual turnover rate of about $7 \%$, this strikes us as manageable if the policy were phased in over an extended period. The level
of turnover becomes somewhat more problematic ( $17 \%$ or higher) in the simulations with four or more types.

While the degree of disruption varies dramatically among the simulations, all suggest to varying degrees significant teacher resistance. In the homogeneous model, $34 \%$ of teachers (again weighted by years teaching) would be made worse off. With four types this grows to a majority, and with six types almost reaches $80 \%$. Even though results are less extreme when we consider seven, eight or nine types, these three models also estimate the majority of teachers would be made worse off. Even in settings where teachers are not unionized, this would make a transition to this policy difficult.

## 7 Conclusion

This paper contributes both to our substantive understanding of reforming teacher compensation and to the practice of structural modeling.

With respect to the latter, it is widely recognized that the strength of structural modeling is that it allows us to consider experiments that lie outside the data. It is equally widely recognized that the validity of the experiment relies on the model being (at least approximately) correct. We show that establishing that a model fits well within sample is, at best, weak evidence that it is approximately correct. Even showing by way of cross-validation that it fits well out-of-sample should not be convincing. In our case, even a model with no unobserved heterogeneity appears to fit well within sample and does reasonably well in cross-validation. It would be easy to conclude that allowing for two or three types is adequate to fit the data. But more formal methods do not support this conclusion. The Bayesian Information Criterion favors seven types. When we rank models in terms of their performance in
cross-validation, we also conclude that we need many types. Even though we cannot reject that eight types is better than seven or that nine types is better than eight, in an informal sense, the differences between the two pairs of models are not large. As we show, the conclusions we draw from our experiment can depend crucially on choosing among models, all of which appear to fit well both within and out-of-sample. Interestingly, the simulations with seven or more types (i.e., when approaching what we believe is the requisite number of types) provide similar results.

On occasion, we have been asked why our model requires so much unobserved heterogeneity. Our first response is that we only appear to require an unusually large number of types because researchers have typically stopped when they were no longer able to converge their models with more unobserved heterogeneity or when the insample fit looked 'good enough.' Had we used the latter rule, we could easily have concluded our search for a satisfactory model with far fewer than seven or nine types. Our second response is that in some ways it should be surprising that we can fit the data well with so few types. After all, we are trying to capture covariance among four equation errors and serial correlation for these four errors. We might expect that we would need at least ten types. And by some measures, we have indeed found that even nine types is inadequate and have not shown that nine types performs better out of sample than ten types would. While any strong conclusion must await similar exercises with other structural models, our working hypothesis is that many policy simulations rely on models that would not be 'good enough' if they were subjected to the type of out-of-sample testing that is common in big data.

With respect to reforming teacher compensation, we establish that, among college graduates, teachers are not only drawn disproportionately from the lower part of the AFQT distribution, but they are also more risk-averse than their counterparts outside teaching. When we allow for unobserved heterogeneity, the low mean AFQT score
among teachers reflects not a low return to cognitive skill within teaching but low returns to other skills, correlated with AFQT. The compression of earnings within teaching attracts relatively risk-averse individuals.

We show that if it were possible to revise compensation in teaching to mimic the return to skills and riskiness of the non-teaching sector, there would be a modest increase in average teachers' AFQT and a modest decrease in average risk aversion. ${ }^{21}$ However, such a shift would adversely affect many of those who are currently in teaching and who would suffer large utility losses if they shifted out of teaching. This makes the process of reform challenging.

[^20]
*Translated into 2012 dollars.

Figure 1: Teachers and Non-teachers earnings* by age


Figure 2: Percentage of teachers by age


Figure 3: Percentage of non-teachers by age


Figure 4: Log earnings by age

(a) Non-teachers

(b) Teachers

Figure 5: Root mean squared error

Table 1: Summary statistics

|  | Teachers <br> $(1)$ | Non-teachers <br> $(2)$ | Not working <br> $(3)$ |
| :---: | :---: | :---: | :---: |
| Earnings | 51.1 | 76.6 | - |
| in $\$ 1,000$ | $(1.3)$ | $(1.4)$ | - |
| Risk aversion | 0.3008 | -0.0389 | 0.0197 |
| standardized | $(0.0178)$ | $(0.0071)$ | $(0.0346)$ |
| Schooling | 17.4 | 16.8 | 16.7 |
| in years | $(0.0)$ | $(0.0)$ | $(0.0)$ |
| AFQT | -0.3061 | 0.0367 | 0.0518 |
| standardized | $(0.0205)$ | $(0.0069)$ | $(0.0343)$ |
|  |  |  |  |
| Individuals | 220 | 1050 | 371 |
| Observations | 2,591 | 20,464 | 825 |

Notes: Standard errors in parenthesis. An individual might be in all three categories.

Table 2: Transition matrix (percentages)

|  |  | $t$ |  |  |
| :--- | :--- | :---: | :---: | :---: |
|  |  | Teacher | Non-teacher | Not working |
| $t-1$ | Teacher | Non-teacher | 03.3 | 5.2 |
|  | Not working | 4.8 | 98.3 | 1.5 |
|  |  |  | 23.5 | 71.6 |

Table 3: Bayesian Information Criterion

|  | BIC | Difference |
| :--- | :---: | :---: |
|  |  |  |
| One type | 24,880 | $-4,958$ |
| Two types | 19,922 | $-1,765$ |
| Three types | 18,157 | -617 |
| Four types | 17,540 | -142 |
| Five types | 17,398 | -156 |
| Six types | 17,242 | -138 |
| Seven types | 17,104 | 1 |
| Eight types | 17,014 | 118 |
| Nine types | 17,132 |  |

Table 4: Occupation specific utility function parameters


Table 5: Occupation specific utility function parameters by type

|  |  |  | One type |  | Seven types |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Coefficient | Stand. Error | Coefficient | Stand. Error |
| Type 1 | constant $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers Non-teachers | $\begin{aligned} & \hline 24.1067^{* * *} \\ & 23.7474^{* * *} \\ & 1.5810^{* * *} \\ & -0.0402^{* * *} \end{aligned}$ | $(1.9166)$ $(1.5050)$ $(0.1088)$ $(0.0041)$ | $\begin{array}{\|l\|} \hline 28.9967^{* * *} \\ 31.6067^{* * *} \\ 0.9897^{* * *} \\ -0.0061 \end{array}$ | $(2.6967)$ $(2.2058)$ $(0.2626)$ $(0.0092)$ |
| Type 2 | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers <br> Non-teachers |  |  | $\begin{array}{\|l\|} \hline 1.6479 \\ -2.6042 \\ 3.2084^{* * *} \\ -0.1363^{* * *} \end{array}$ | $\begin{aligned} & (2.1350) \\ & (2.0928) \\ & (0.5728) \\ & (0.0516) \end{aligned}$ |
| Type 3 | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers Non-teachers |  |  | $\begin{array}{\|l\|} \hline 6.4219^{* * *} \\ 1.0854 \\ 1.9310^{* *} \\ 0.0298 \end{array}$ | $(2.2981)$ $(2.4902)$ $(0.9432)$ $(0.1094)$ |
| Type 4 | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers Non-teachers |  |  | $\begin{array}{\|l\|} \hline 4.5618^{* *} \\ -2.4229 \\ 0.8402^{* * *} \\ -0.0065 \\ \hline \end{array}$ | $(2.0874)$ $(2.3522)$ $(0.2367)$ $(0.0063)$ |
| Type 5 | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers Non-teachers |  |  | $\begin{aligned} & \hline-1.7169 \\ & -8.8825^{* * *} \\ & 2.4700^{* * *} \\ & -0.0618^{* * *} \end{aligned}$ | $\begin{aligned} & (2.4202) \\ & (2.5508) \\ & (0.3433) \\ & (0.0118) \end{aligned}$ |
| $\text { Type } 6$ | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers <br> Non-teachers |  |  | $\begin{array}{\|l\|} \hline-2.4901 \\ -7.4707^{* * *} \\ 3.8278^{* * *} \\ -0.1642^{* * *} \end{array}$ | $(1.8972)$ $(1.8423)$ $(0.3536)$ $(0.0232)$ |
| $\text { Type } 7$ | interaction $\begin{aligned} & E[w] \\ & E[w]^{2} \end{aligned}$ | Teachers <br> Non-teachers |  |  | $\begin{aligned} & \hline-0.7483 \\ & -6.1109^{* * *} \\ & 2.4667^{* * *} \\ & -0.0574^{* * *} \end{aligned}$ | $(1.9378)$ $(1.9234)$ $(0.3142)$ $(0.0165)$ |

Table 6: Log earnings parameters

|  |  | One type |  | Seven types |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Coefficient | Stand. Error | Coefficient | Stand. Error |
| $\begin{aligned} & \hline \text { AFQT } \\ & \quad \text { percentile } \end{aligned}$ | Teachers | -0.0005** | (0.0002) | $0.0017^{* * *}$ | (0.0003) |
|  | Non-teachers | $0.0041^{* * *}$ | (0.0001) | $0.0034^{* * *}$ | (0.0003) |
| Schooling | Teachers | $0.1053^{* * *}$ | (0.0046) | $0.0878^{* * *}$ | (0.0045) |
|  | Non-teachers | 0.0689*** | (0.0014) | $0.0633^{* * *}$ | (0.0025) |
| Male dummy | Teachers | 0.0332* | (0.0180) | 0.0906*** | (0.0295) |
|  | Non-teachers | $0.1590^{* * *}$ | (0.0066) | $0.0896 * * *$ | (0.0140) |
| Married dummy | Teachers | 0.0186 | (0.0209) | -0.0223 | (0.0225) |
|  | Non-teachers | 0.0692*** | (0.0090) | $0.0296 * * *$ | (0.0109) |
| Married $\times$ male | Teachers | 0.0665 | (0.0543) | -0.0123 | (0.0497) |
|  | Non-teachers | 0.0354*** | (0.0118) | 0.0493 *** | (0.0133) |
| Children dummy | Teachers | -0.1131*** | (0.0215) | $-0.1511^{* * *}$ | (0.0176) |
|  | Non-teachers | $-0.0507^{* * *}$ | (0.0089) | $-0.0565 * * *$ | (0.0098) |
| Children $\times$ male | Teachers | 0.0857 | (0.0570) | $0.1186^{* * *}$ | (0.0446) |
|  | Non-teachers | $0.1326^{* * *}$ | (0.0112) | $0.1469 * * *$ | (0.0116) |
| Experience teaching | Teachers | 0.0372*** | (0.0036) | 0.0397*** | (0.0028) |
|  | Non-teachers | -0.0031 | (0.0024) | 0.0066*** | (0.0017) |
| Experience teaching ${ }^{2}$ | Teachers | $-0.0004^{* * *}$ | (0.0002) | $-0.0006^{* * *}$ | (0.0001) |
|  | Non-teachers | $0.0011^{* * *}$ | (0.0002) | $0.0006 * * *$ | (0.0001) |
| Experience non-teaching | Teachers | $0.0266^{* * *}$ | (0.0021) | $0.0274^{* * *}$ | (0.0020) |
|  | Non-teachers | $0.0811^{* * *}$ | (0.0018) | 0.0760*** | (0.0016) |
| Experience non-teaching ${ }^{2}$ | Teachers | $-0.0008^{* * *}$ | (0.0001) | $-0.0007^{* * *}$ | (0.0001) |
|  | Non-teachers | $-0.0016^{* * *}$ | (0.0001) | $-0.0015^{* * *}$ | (0.0000) |
| $\sigma_{A}$ | Teachers | $0.2272^{* * *}$ | (0.0163) | $0.3743^{* * *}$ | (0.0146) |
|  | Non-teachers | $0.1948 * * *$ | (0.0084) | $0.2651 * * *$ | (0.0052) |
| $\sigma_{B}$ | Teachers | 0.0030*** | (0.0004) | $-0.0042^{* * *}$ | (0.0004) |
|  | Non-teachers | $0.0083 * * *$ | (0.0002) | 0.0018*** | (0.0001) |
| constant | Teachers | 8.5231*** | (0.0835) | 9.5617*** | (0.0895) |
|  | Non-teachers | $8.7513^{* * *}$ | (0.0255) | $9.1146^{* * *}$ | (0.0450) |

Notes: Trend, trend squared and race dummies were also included. Interactions for the the other six types are not shown.

Table 7: Transition matrix of real and predicted choices (percentages)


Table 8: Average standardized risk aversion and AFQT transitions


Note: * means the population average is statistically different from the point estimate using SE clustered at the individual level.

Table 9: Maximum $t$-statistic of the 20 draws


Note: ${ }^{* *}$ denotes cells where averages are statistically different, * denotes cells where averages could be statistically different.

|  | $\begin{aligned} & \hline \hline \text { AFQT } \\ & \text { (stand } \end{aligned}$ | Risk av. rdized) | Age | Male | Black | Hispanic | $\begin{gathered} \hline \text { Earnings } \\ \text { (in } \$ 1,000 \text { ) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DATA | $\begin{aligned} & -0.3067 \\ & (0.0205) \end{aligned}$ | $\begin{gathered} 0.2967 \\ (0.0175) \end{gathered}$ | $\begin{aligned} & 37.8 \\ & (0.2) \end{aligned}$ | $\begin{gathered} 0.2578 \\ (0.0086) \end{gathered}$ | $\begin{gathered} 0.1690 \\ (0.0074) \end{gathered}$ | $\begin{gathered} 0.1382 \\ (0.0068) \end{gathered}$ | $\begin{aligned} & 51.1 \\ & (0.7) \end{aligned}$ |
| One type | $\begin{gathered} 0.1162^{* * *} \\ (0.0131) \end{gathered}$ | $\begin{gathered} -0.0233^{* * *} \\ (0.0071) \end{gathered}$ | $\begin{gathered} 0.0 \\ (0.1) \end{gathered}$ | $\begin{gathered} 0.0040^{* * *} \\ (0.0011) \end{gathered}$ | $\begin{gathered} -0.0222^{* * *} \\ (0.0026) \end{gathered}$ | $\begin{gathered} -0.0041^{* * *} \\ (0.0005) \end{gathered}$ | $\begin{gathered} 2.8^{* *} \\ (1.2) \end{gathered}$ |
| Two types | $\begin{gathered} 0.0410^{* * *} \\ (0.0113) \end{gathered}$ | $\begin{gathered} -0.0176^{* * *} \\ (0.0062) \end{gathered}$ | $\begin{gathered} -0.2^{* * *} \\ (0.1) \end{gathered}$ | $\begin{gathered} -0.0064^{* * *} \\ (0.0018) \end{gathered}$ | $\begin{gathered} -0.0066^{* * *} \\ (0.0022) \end{gathered}$ | $\begin{gathered} -0.0020^{* * *} \\ (0.0007) \end{gathered}$ | $\begin{gathered} 3.9 * * * \\ (1.1) \end{gathered}$ |
| Three types | $\begin{aligned} & -0.0023 \\ & (0.0089) \end{aligned}$ | $\begin{gathered} -0.0183^{* *} \\ (0.0087) \end{gathered}$ | $\begin{gathered} -0.3^{* * *} \\ (0.1) \end{gathered}$ | $\begin{gathered} -0.0047^{* * *} \\ (0.0016) \end{gathered}$ | $\begin{aligned} & -0.0026 \\ & (0.0021) \end{aligned}$ | $\begin{gathered} 0.0011 \\ (0.0008) \end{gathered}$ | $\begin{gathered} 3.4^{* * *} \\ (1.1) \end{gathered}$ |
| Four types | $\begin{gathered} 0.0023 \\ (0.0207) \end{gathered}$ | $\begin{gathered} -0.0391^{* *} \\ (0.0165) \end{gathered}$ | $\begin{gathered} -0.4^{* *} \\ (0.2) \end{gathered}$ | $\begin{gathered} 0.0012 \\ (0.0067) \end{gathered}$ | $\begin{aligned} & -0.0031 \\ & (0.0047) \end{aligned}$ | $\begin{aligned} & -0.0040 \\ & (0.0027) \end{aligned}$ | $\begin{gathered} 4.3^{* * *} \\ (1.1) \end{gathered}$ |
| Five types | $\begin{gathered} 0.3554^{* * *} \\ (0.0488) \end{gathered}$ | $\begin{gathered} -0.2564^{* * *} \\ (0.0212) \end{gathered}$ | $\begin{gathered} -2.5^{* * *} \\ (0.2) \end{gathered}$ | $\begin{gathered} 0.2137 * * * \\ (0.0344) \end{gathered}$ | $\begin{gathered} -0.0544^{* * *} \\ (0.0092) \end{gathered}$ | $\begin{gathered} -0.0404^{* * *} \\ (0.0073) \end{gathered}$ | $\begin{gathered} 9.4^{* * *} \\ (1.6) \end{gathered}$ |
| Six types | $\begin{gathered} 0.2335^{* * *} \\ (0.0526) \end{gathered}$ | $\begin{gathered} -0.1489 * * * \\ (0.0278) \end{gathered}$ | $\begin{gathered} -1.2^{* * *} \\ (0.2) \end{gathered}$ | $\begin{gathered} 0.1298 * * * \\ (0.0319) \end{gathered}$ | $\begin{gathered} -0.0406^{* * *} \\ (0.0088) \end{gathered}$ | $\begin{gathered} -0.0186^{* * *} \\ (0.0062) \end{gathered}$ | $\begin{gathered} 10.4^{* * *} \\ (1.8) \end{gathered}$ |
| Seven types | $\begin{gathered} 0.0746^{* *} \\ (0.0316) \end{gathered}$ | $\begin{gathered} -0.0396^{* * *} \\ (0.0139) \end{gathered}$ | $\begin{gathered} -0.5^{* *} \\ (0.2) \end{gathered}$ | $\begin{gathered} 0.0063 \\ (0.0098) \end{gathered}$ | $\begin{gathered} -0.0145^{* *} \\ (0.0060) \end{gathered}$ | $\begin{aligned} & -0.0046 \\ & (0.0029) \end{aligned}$ | $\begin{gathered} 2.5^{* *} \\ (1.2) \end{gathered}$ |
| Eight types | $\begin{gathered} 0.1187^{* * *} \\ (0.0351) \end{gathered}$ | $\begin{gathered} -0.0586^{* * *} \\ (0.0176) \end{gathered}$ | $\begin{gathered} -0.7^{* * *} \\ (0.2) \end{gathered}$ | $\begin{gathered} 0.0340 * * \\ (0.0133) \end{gathered}$ | $\begin{gathered} -0.0181^{* * *} \\ (0.0066) \end{gathered}$ | $\begin{gathered} -0.0070^{* * *} \\ (0.0027) \end{gathered}$ | $\begin{gathered} 3.8^{* *} \\ (1.5) \end{gathered}$ |
| Nine types | $\begin{gathered} 0.1048 * * \\ (0.0458) \\ \hline \end{gathered}$ | $\begin{gathered} -0.0595^{* *} * \\ (0.0195) \\ \hline \end{gathered}$ | $\begin{gathered} -1.1^{* * *} \\ (0.2) \\ \hline \end{gathered}$ | $\begin{aligned} & -0.0005 \\ & (0.0226) \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.0132 \\ & (0.0109) \\ & \hline \end{aligned}$ | $\begin{gathered} -0.0056 \\ (0.0044) \\ \hline \end{gathered}$ | $\begin{aligned} & 3.1^{*} \\ & (1.7) \\ & \hline \hline \end{aligned}$ |

[^21]
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[^0]:    *We are grateful to Peter Arcidiacono, Richard Blundell, Ivan Fernandez-Val, Hiro Kaido, Zhongjun Qu and Marc Rysman for helpful discussions and to participants in in the Cowles Foundation Conference on Structural Microeconomics and seminars at Arizona State, Boston University, Brandeis University, Carleton University, Duke the Federal Reserve Bank of Minneapolis; the International Symposium on Contemporary Labor Economics (Jinan University), the Minneapolis Fed, Queen's University, SOLE, UCSD, the University of Connecticut, the University of Western Ontario and Washington University in Saint Louis for their comments and suggestions. Lang acknowledges NSF funding under grant SES-1260917. The usual caveat applies.
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[^1]:    ${ }^{1}$ There is an enormous literature on the decisions to become a teacher and to leave teaching which we will not attempt to review thoroughly. This literature is reviewed in Dolton (2006).

[^2]:    ${ }^{2}$ Leigh (2012) finds evidence that higher pay increases the test scores of students in teacher training programs in Australia and some evidence that greater earnings dispersion outside of teaching lowers scores.
    ${ }^{3}$ See Biasi (2017) for a study of teacher mobility and exit following Wisconsin's Act 10, which radically overhauled the compensation system for teachers in that state.

[^3]:    ${ }^{4}$ In 2012 dollars.

[^4]:    ${ }^{5} 1993,2002,2004$ and 2006.

[^5]:    ${ }^{6}$ Individuals that have at least 17 years of schooling.

[^6]:    ${ }^{7}$ We assume that utility is quadratic in earnings and earnings equal expected earnings plus a mean zero shock with a given variance. Thus, expected utility is a function of expected earnings and expected earnings squared.

[^7]:    ${ }^{8}$ As discussed in the next section, schooling is occupation specific.

[^8]:    ${ }^{9}$ As commented by Aguirregabiria and Mira (2010) the discount factor in most applications is not estimated because it is poorly identified (e.g., see Rust (1987)).

[^9]:    ${ }^{10}$ See Keane and Wolpin (1997), Eckstein and Wolpin (1999) and Arcidiacono (2004) for other papers that control for unobserved heterogeneity in dynamic discrete choice models. Stinebrickner (2001a) uses this approach in a closely related model of occupational choice by qualified teachers.

[^10]:    ${ }^{11} B I C=-2 \cdot \log$ likelihood $+d \cdot \log (N)$, where $N$ is the sample size and $d$ is the total number of parameters.

[^11]:    ${ }^{12} \mathrm{We}$ did not get convergence on two of the 20 subsamples for the nine-type model, so we drew two additional subsamples, converged all nine models with the two new samples and used those to compare the nine-type model with the other models.

[^12]:    ${ }^{13} \mathrm{We}$ do not take the concept of type literally but as a way of accounting for correlation among equation errors and over time. Each individual has a posterior probability of being each type based on the prior probabilities and her earnings and occupation choices. Using these weighted averages only 12 observations are estimated to have negative marginal utility of earnings $(0.08 \%$ of the observations that have earnings data).

[^13]:    ${ }^{14}$ We expect that this reflects very experienced teachers transitioning to other well-paid jobs in education.

[^14]:    ${ }^{15}$ Interestingly, using a different model and data set Wiswall (2007) also finds a strong positive correlation between unmeasured skills outside and within teaching; and that there is more variation in earnings across types outside than within teaching.

[^15]:    ${ }^{16}$ Using standard errors clustered at the individual level to account for possible correlation of observations.

[^16]:    ${ }^{17}$ The surprising ability to fit the sawtooth pattern at older ages reflects the fact that older workers are only observed in later surveys which were conducted only every other year. Thus the sample for 42 and 44 year olds is roughly constant and disjoint from the one for 43 and 45 year olds. The predictions in each case rely on the observations from in the relevant age group.

[^17]:    ${ }^{18}$ Using standard errors clustered at the individual level.

[^18]:    ${ }^{19}$ We make this adjustment because we would not anticipate that the expected utility of riskneutral individuals to be affected by the increased riskiness. Given the phrasing of the question, we know only that this group has a low degree of risk aversion and not that its members are risk neutral.

[^19]:    ${ }^{20}$ For instance, a Hausman test comparing the effects of the policy using the model with N and $\mathrm{N}+1$ types does not have the usual chi-squared distribution.

[^20]:    ${ }^{21}$ Both effects are statistically insignificant for models with enough heterogeneity.

[^21]:    Note: SE are calculated using parametric bootstrapping with 100 draws.

