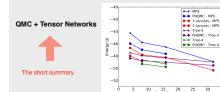
Stochastic Projection + Tensor Networks



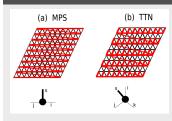
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Abstract

We apply a series of projection techniques on top of tensor networks to compute energies of ground state wave functions with higher accuracy than tensor networks alone with minimal additional cost. We consider both matrix product states as well as tree tensor networks in this work. Building on top of these approaches, we apply fixed-node quantum Monte Carlo, Lanczos steps, and exact projection. We demonstrate these improvements for the triangular lattice Heisenberg model, where we capture up to 57% of the remaining energy not captured by the tensor network alone. We conclude by discussing further wavs to improve our approach.



Wave functions



Tensor Networks

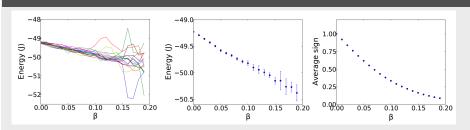
- · Matrix product states
- Tree tensor networks: TTN have physical indices at the nodes of the tree.
 They can capture significant local entanglement structure missed by MPS. In our tests, they capture 30-40% of the energy missed by MPS for the same bond dimension!

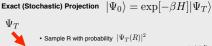
Test System

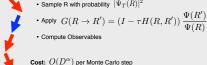
- Heisenberg Model on a Triangular Lattice
- 10 x 10 lattice
- · open boundary conditions

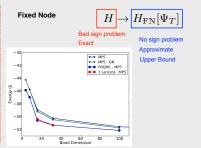


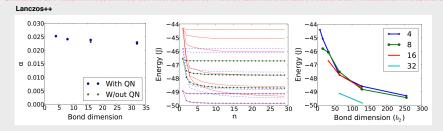
Methods











Basis: $\{|\Psi\rangle,H|\Psi\rangle,H^2|\Psi\rangle,H^3|\Psi\rangle,H^4|\Psi\rangle,...\}$

Solve: $H|\Psi\rangle=ES|\Psi\rangle$ in this basis

Exactly: 3 basis elements

Approximately: 30 basis elements

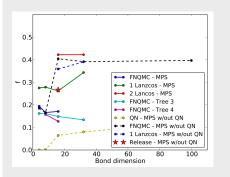
Ways to (exactly) compute basis

- MPS/MPO Formalism
- · Quantum Monte Carlo
- Hybrid QMC/MPO

Way to (approximately) compute basis

- Apply $H|\Psi
 angle$ via MPO
- Truncate to smaller bond dimension b2
- Iterate

Results



Conclusions

These 4 approaches allow us to push beyond what is possible with tensor networks alone. We believe future applications using PEPS and other tensor networks will show even more significant gains.

Exact (Stochastic) Projection

Fixed Node

Exact Lanczos (3 basis elements)

Approximate Lanczos (30 basis elements)

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