

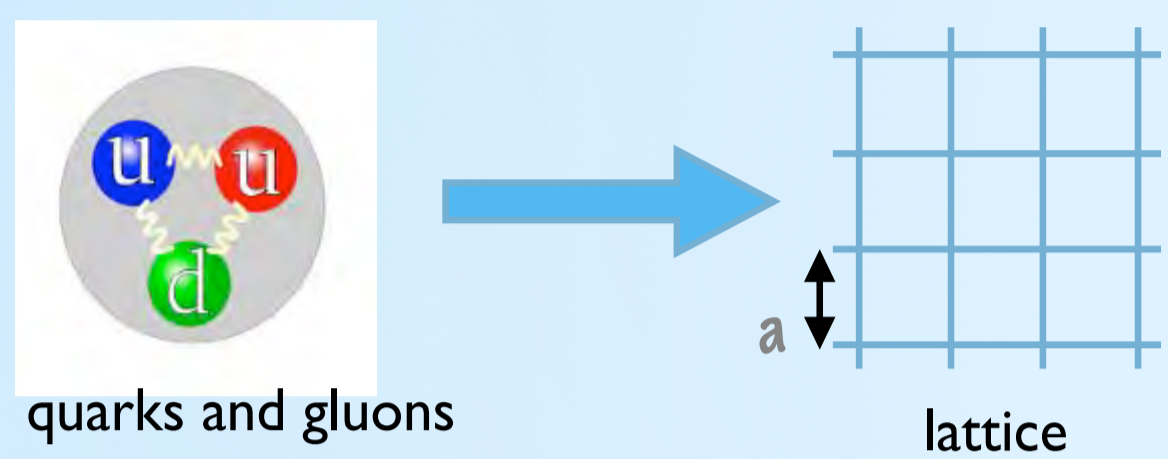
# Classical and Quantum Simulation of Gauge Theories



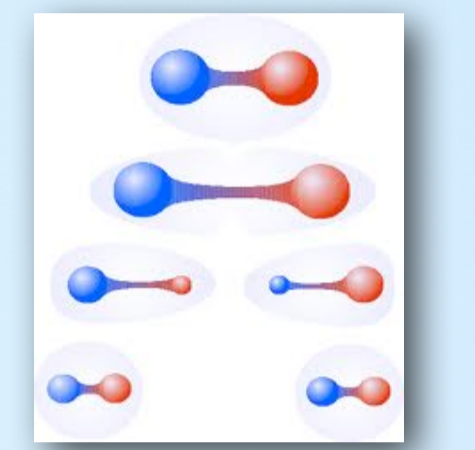
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We show how to simulate models with *gauge symmetry* in the lattice using *atomic and quantum optics* tools and *tensor network* methods. The construction is based on *quantum links* that realize continuous gauge symmetry with discrete quantum variables. At low energies, quantum link models with staggered fermions emerge from a Hubbard-type model that can be quantum simulated. These systems share qualitative features with *quantum chromodynamics*, including *chiral symmetry breaking* and restoration at non-zero temperature or baryon density. This allows us to investigate *string breaking* as well as the *real-time evolution* after a quench in gauge theories.

The study of Gauge theories is the study of Nature.



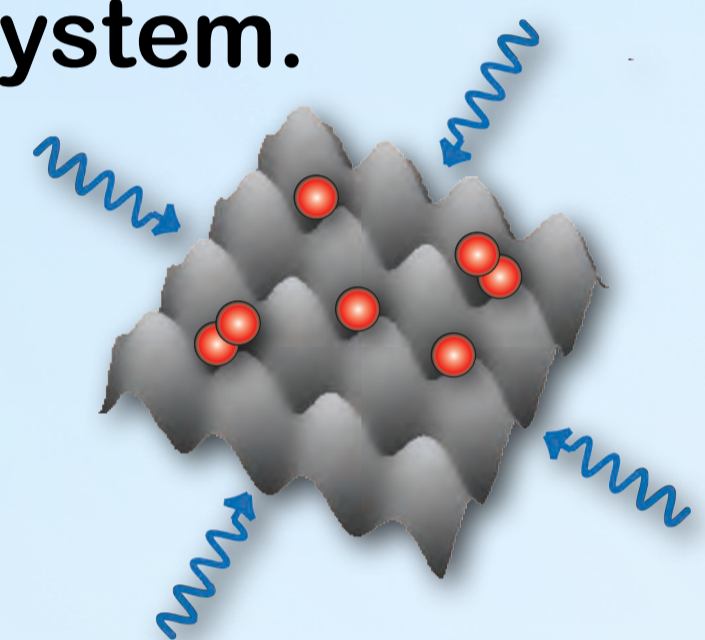
**Gauge symmetry as a fundamental principle**  
 Standard model: For every force, there is a gauge boson  
**Gauge symmetry as an emergent phenomenon**  
 Better understanding of spin-liquids and quantum magnetism  
**Gauge symmetry as a resource**



String breaking

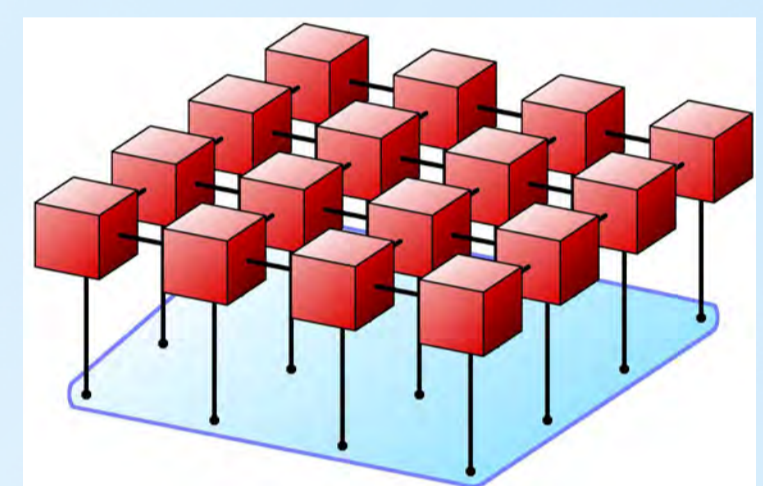
Use the low-energy properties of these systems to implement any quantum information task.

**Feynman's universal quantum simulator:** controlled quantum device which efficiently reproduces the dynamics of any other many-particle quantum system.



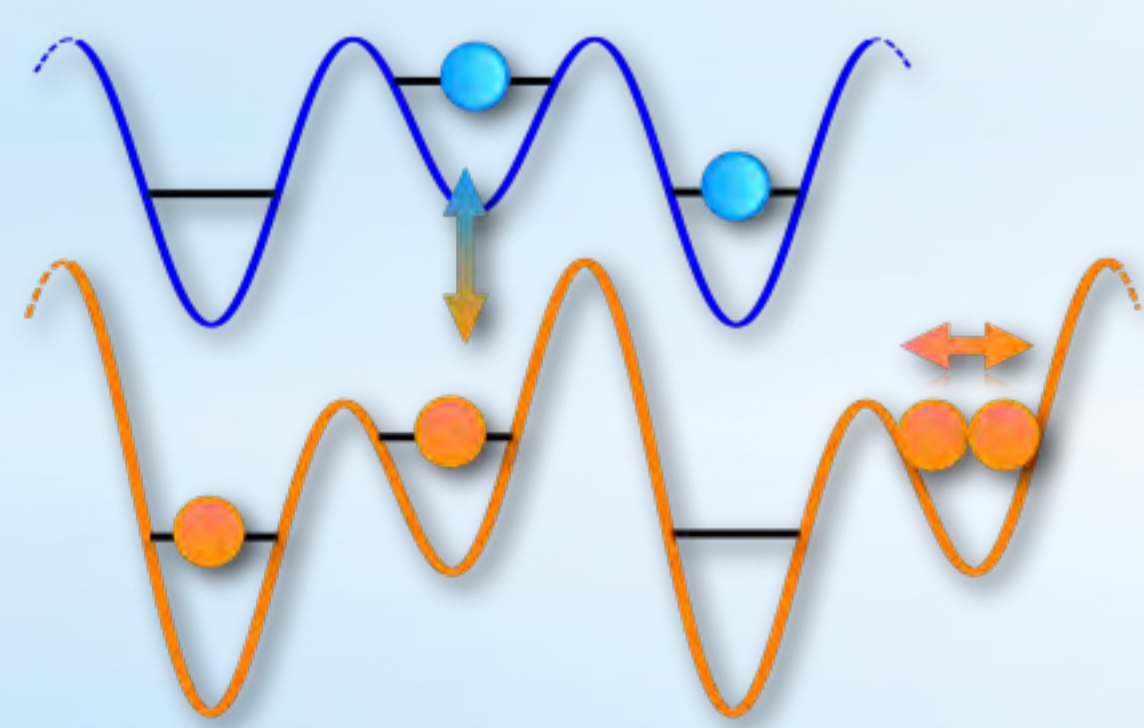
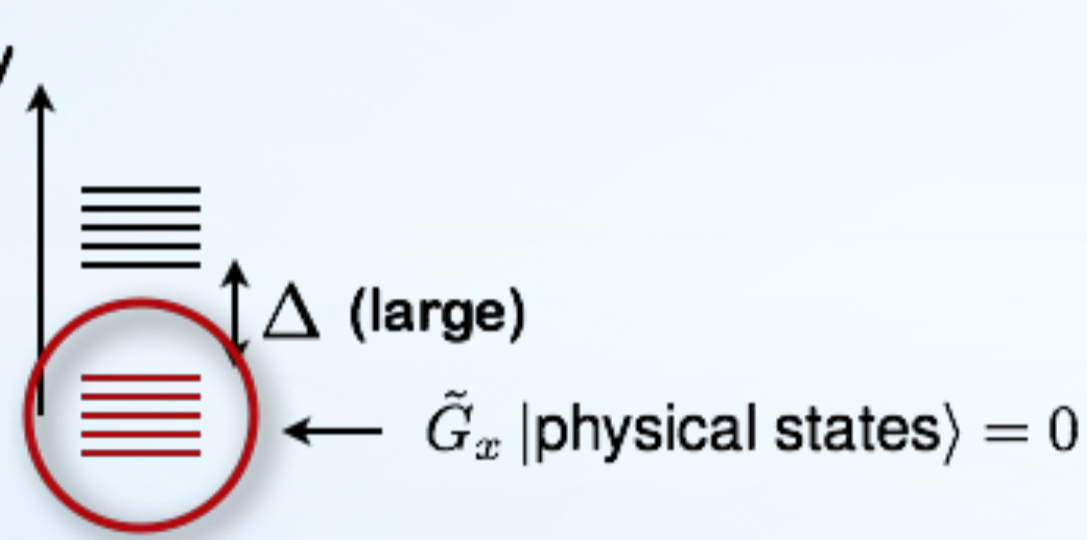
How?... cold atoms, ions, photons, superconducting circuit, etc.

**Tensor network methods:** variational ansatz for quantum many-body states describing the local degrees of freedom in real space  
 Direct access to entanglement  
 Dynamics of quantum many-body states in- and-out of equilibrium  
 Control of global and local (gauge) symmetry

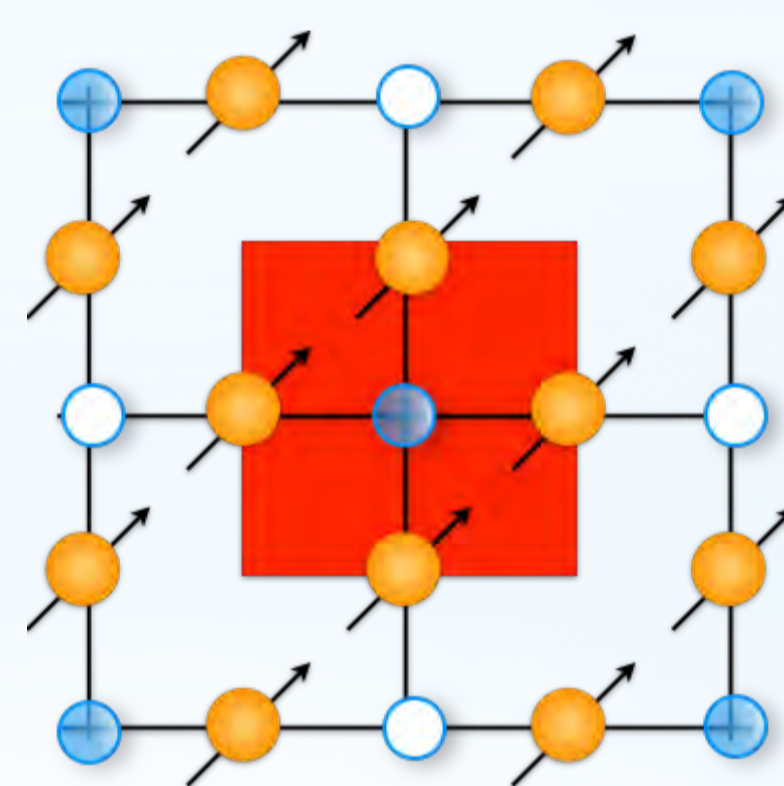


**Bose + Fermi Hubbard model**

$$H_{\text{microscopic}} = \Delta \sum_x G_x^2 + \dots$$



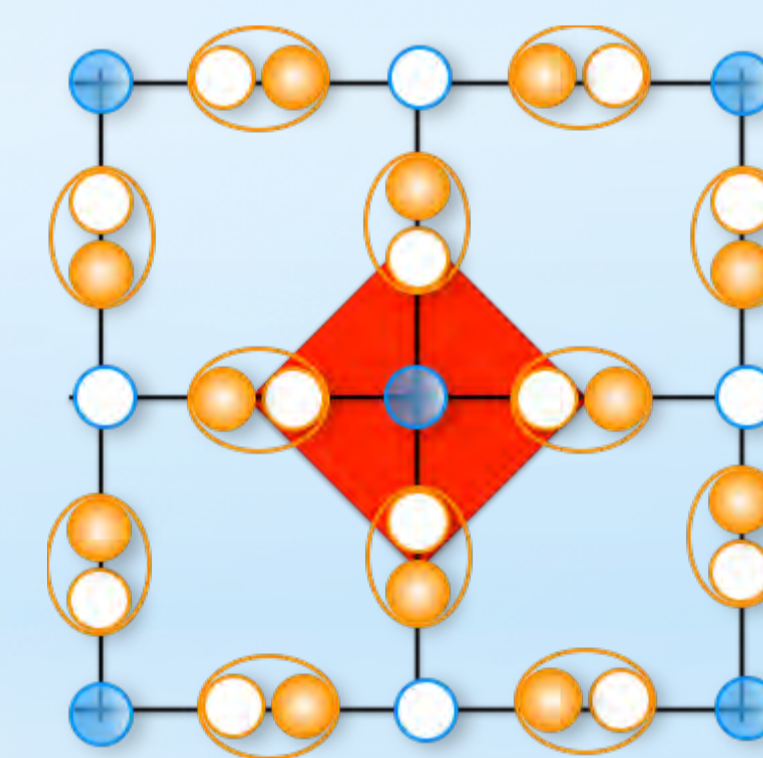
**Quantum link models**



$$G_{\text{vert}} |\text{phys}\rangle = 0$$

$$G_{\text{vert}} |s_{\text{vert}}\rangle = 0$$

$$|s_{\text{vert}}\rangle = \sum_{n_c, n_\psi} A_{n_c, n_\psi}^{(s_{\text{vert}})} |n_c, n_\psi\rangle$$



$$|\text{phys}\rangle = \sum_{s_1, \dots, s_x, \dots} a(s_1, \dots, s_x, \dots) \text{Tr} [A^{(s_1)} \dots A^{(s_x)} \dots] |s_1, \dots, s_x, \dots\rangle$$

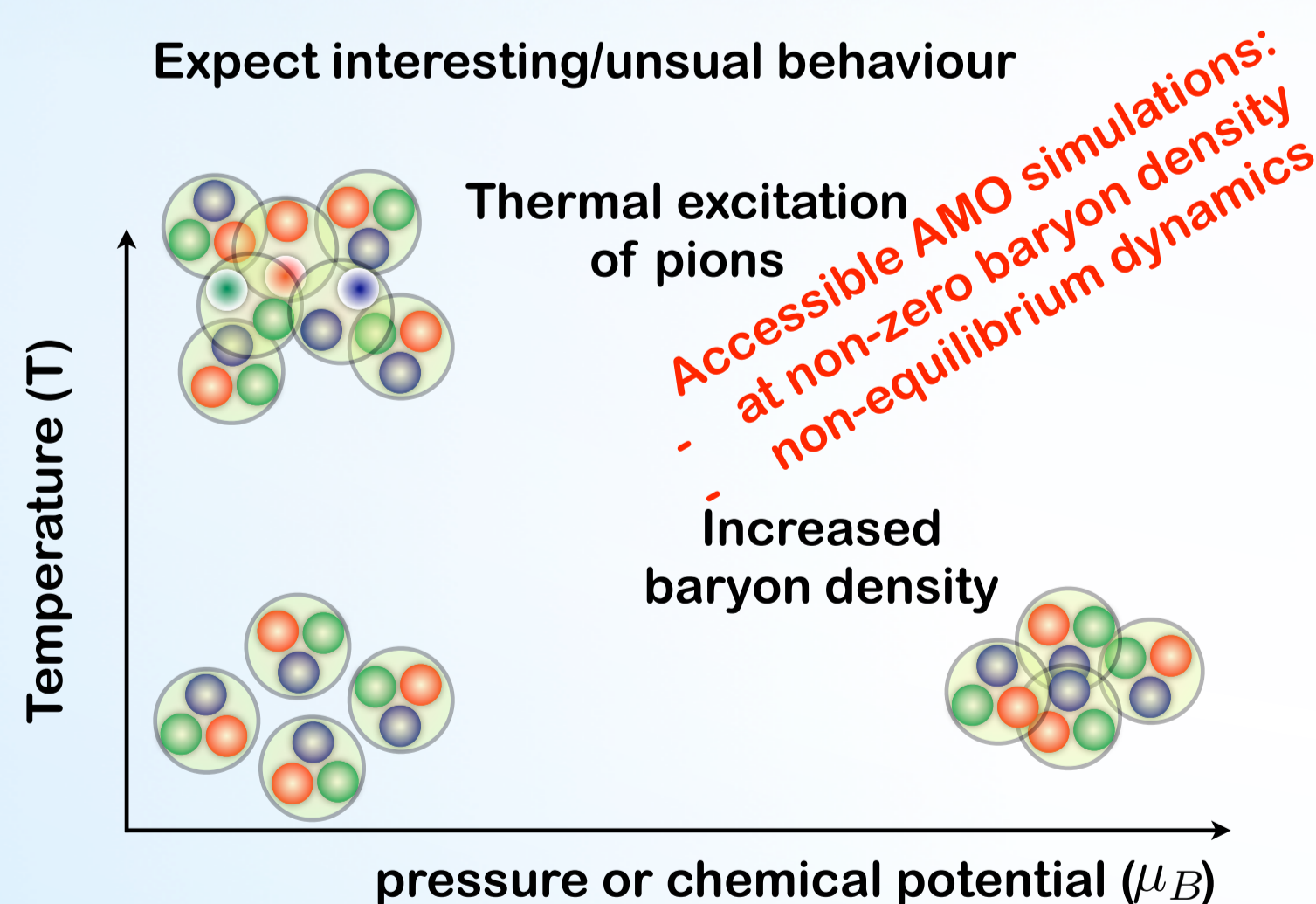
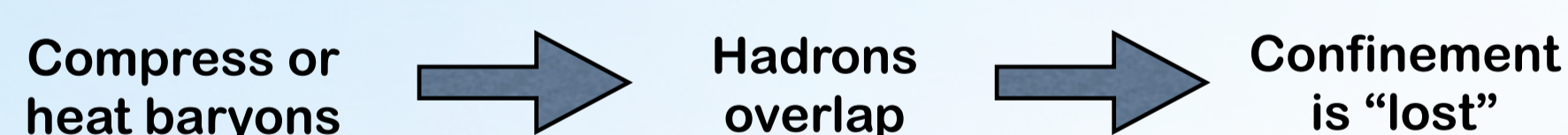
**Emergent lattice gauge theory**

**Exact description of the gauge invariant subspace with tensor networks**

$$H = \frac{g^2}{2} \sum_x E_{x,x+1}^2 - t \sum_x [\psi_x^\dagger U_{x,x+1} \psi_{x+1} + \text{h.c.}] + m \sum_x (-1)^x \psi_x^\dagger \psi_x$$

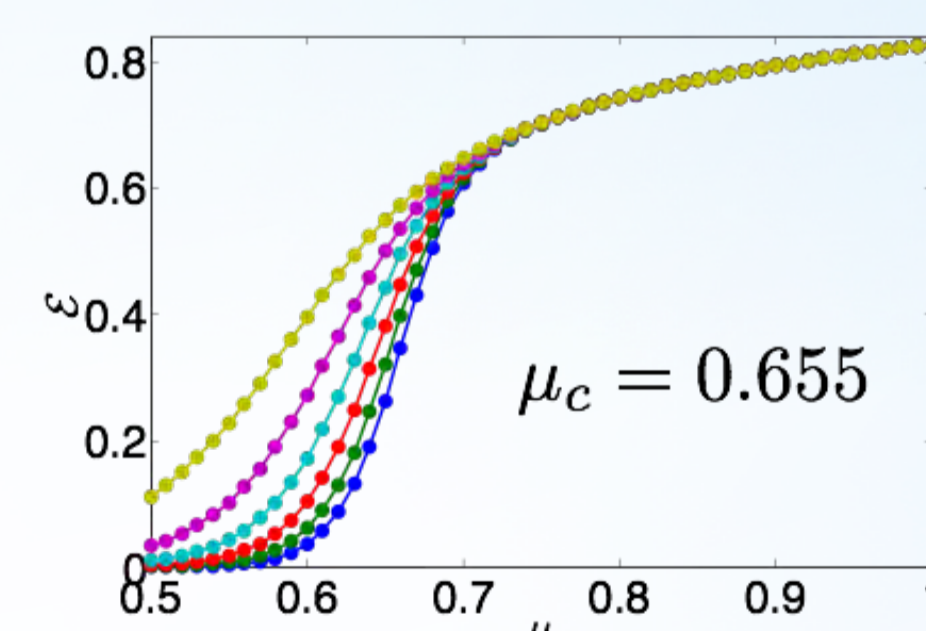
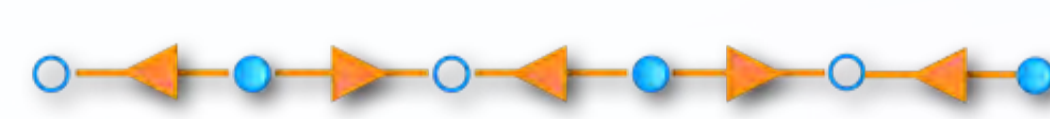
$$H = \frac{g^2}{2} \sum_x (S_{x,x+1}^z)^2 - t \sum_x [\psi_x^\dagger S_{x,x+1}^+ \psi_{x+1} + \text{h.c.}] + m \sum_x (-1)^x \psi_x^\dagger \psi_x$$

QCD under extreme conditions



CP symmetry breaking in QED<sub>2</sub>

$$\mu < 0: \mathcal{E} = \sum_x E_{x,x+1} = 0$$

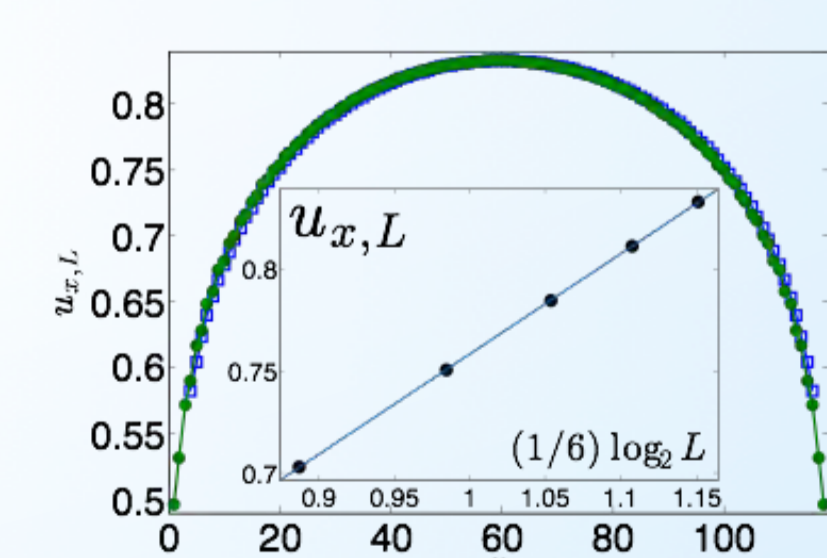
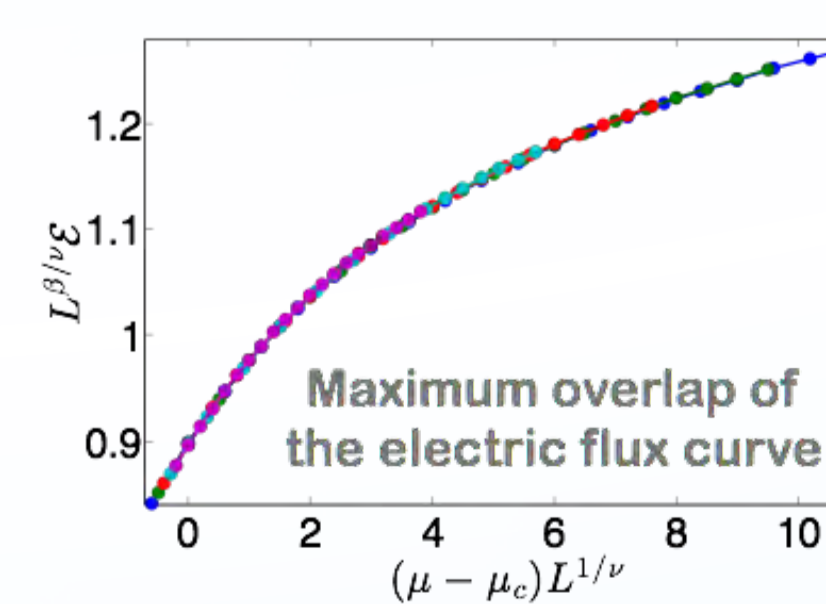


$$\mu > 0: \mathcal{E} = \sum_x E_{x,x+1} \neq 0$$

Total electric flux

Second order phase transition: Parity and charge conjugation spontaneously broken (Ising universality class)

Critical exponents:  
 $\beta = \frac{1}{8}$      $\nu = 1$

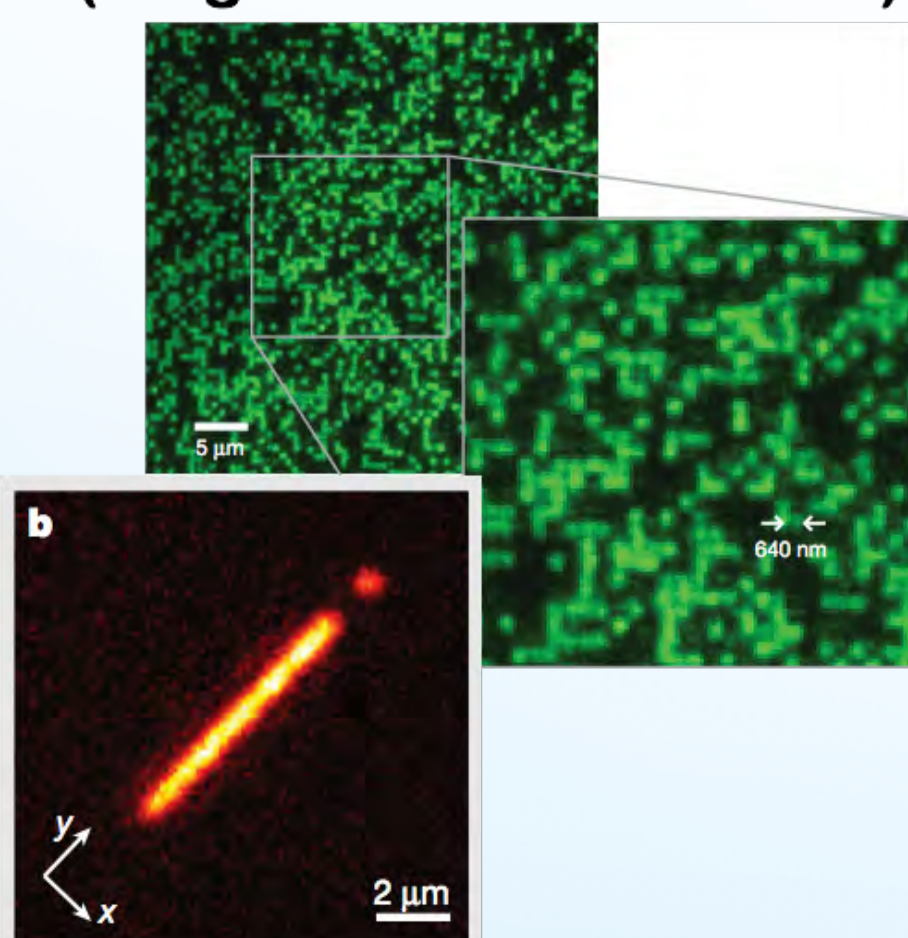
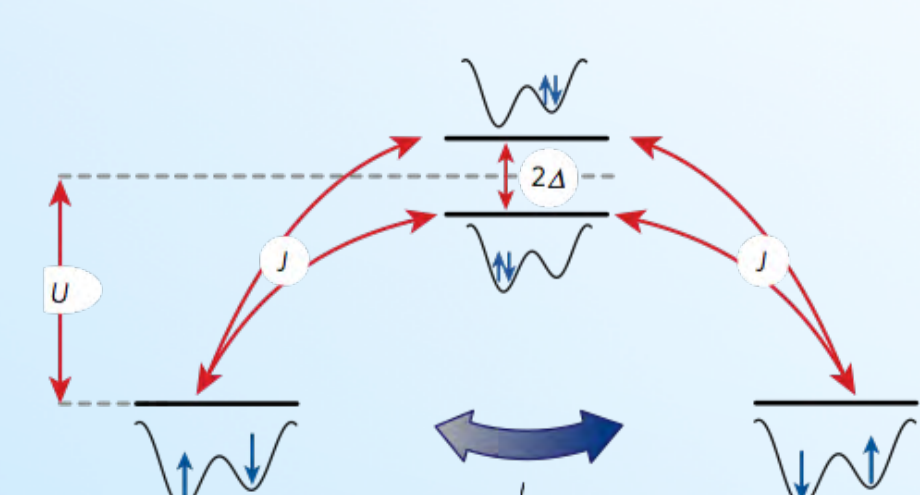


Central charge:  
 $c = \frac{1}{2}$

Preparation of many body states (Mott phase)

Evolution (Super-exchange)

Detection (Single-site fluorescence)



Atomic quantum simulation of dynamical gauge fields coupled to fermionic matter: from string breaking to evolution after a quench, Phys. Rev. Lett. 109, 175302 (2012)

Atomic quantum simulation of U(N) and SU(N) non-abelian lattice gauge theories, Phys. Rev. Lett. 110, 125303 (2013)

Superconducting circuits for quantum simulation of dynamical gauge fields, Phys. Rev. Lett. 111, 110504 (2013)

Tensor networks for Lattice Gauge Theories and Atomic Quantum Simulation, arXiv:1312.3127 (2013)

Related works at ICFO, Barcelona (M. Lewenstein's group) and MPQ, Munich (I. Cirac's group)

