Practical Implementation of TSLSFECLUS Algorithm

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Our algorithm is programmed in SAS for ease of implementation. The main macro that performs the iterative procedure is TSLSFECLUS. This macro can accommodate a wide range of model features such as endogeneity, cluster standard error correction, and multiple high-dimensional fixed effects. In addition, it allows multiple specifications that differ only in their dependent variables to be estimated in a single call. Finally, the macro automatically outputs the number of iterations needed for model convergence together with the model estimates. The macro mainly contains the following four steps.

- 1): Given model specification, identify multiple high-dimensional fixed effects to absorb. Set the values of maximum number of iteration *Maxiter* and the tolerance level *tol*.
- 2): Absorb fixed effects from all dependent and explanatory (including instrumental) variables, one by one until all the fixed effects are absorbed once. Save standardized data S_1 , and the estimated parameters of interest from model S_1 , labeled as $\{\hat{\beta}^{(1)}_{k}\}_{k=1,2,...,K}$.
- 3): Repeat step 2) and record S_2 , and obtain $\{\hat{\beta}^{(2)}_{k}\}_{k=1,2,\dots,K}$ from estimating the model using S_2 .
- 4): Calculate $|\Delta_2| = \max\{|\frac{\widehat{\beta}^{(2)}_k \widehat{\beta}^{(1)}_k}{\widehat{\beta}^{(1)}_k}|\}_{k=1,2,...,K}$, the maximum absolute value of percentage difference between adjacent iterations among K estimated parameters of interest. If $|\Delta_2| < tol$, then stop here and report coefficient estimates $\{\widehat{\beta}^{(2)}_k\}_{k=1,2,...,K}$; otherwise, repeat step 2) until $|\Delta_i| = \max\{|\frac{\widehat{\beta}^{(i)}_k \widehat{\beta}^{(i-1)}_k}{\widehat{\beta}^{(i-1)}_k}|\}_{k=1,2,...,K} < tol$ or the maximum number of iterations have been reached. The reported number of iteration = $\min\{i=\{i||\Delta_i| < tol\}, Maxiter\}$.

For more details of the algorithm, please refer to our working paper "An Iterative Approach to Estimation with Multiple High-Dimensional Fixed Effects: Controlling Simultaneously for Patients, Providers and Counties" (Luo, Zhu and Ellis, Boston University Working Paper, 2017).

Below is a sample call of our two macros in SAS. The second macro can be called directly if only one iteration is desired, such as if there is only one high-dimensional fixed effect:

Libname junk "directory for storing temporary data sets";

```
%auto_iter(
indsn = in_data,
                                  /* input data */
                                  /* tolerance level for convergence */
tol = 0.0001,
                                  /* maximum number of iteration */
maxiter = 10,
                                  /* output data for storing estimates from all iterations */
betasefinal = out_data,
                                  /* number of absorbed fixed effects */
fevarcount = 3,
                                  /* directory for storing temporary data sets */
auto_tempdir = junk,
                                  /* dependent variable */
auto_depvar = y,
                                   /* endogenous variable */
auto\_endog = x,
                                   /* instrumental variable */
auto\_inst = z,
                                   /* exogenous variable */
auto_exog = ,
                                   /* variables defining absorbed fixed effects */
auto_fe = i c t,
                                   /* incremental on iteration number */
auto_FE_iter = 1,
                                   /* variable defining cluster level */
auto\_cluster = c,
                                   /* other variables to be carried along to final dataset
auto_othervar = ,
                                   for final analysis */
auto_regtype = TSLS,
                                   /* TSLS or OLS */
                                   /* yes or no to showing sample summary statistics */
auto_showmeans = no,
                                   /* yes or no to showing reduced form results of TSLS
auto_showrf = no,
                                    model */
                                    /* yes or no to OLS without cluster correction */
auto\_showols = no,
                                   /* yes or no to doing PROC SURVEYREG */
/* yes or no to wide format table */
auto_dosurveyreg = no,
auto_wide = no
);
*which calls the following core macro iteratively;
%TSLSCLUS_iterFE(
runtitle = "TSLS: one fixed effect",
                                            /* running title */
                                    /* input data for each iteration: &indsn. for the first
indata = in_data,
                                    iteration, standardized data for subsequent iterations */
                                    /* dependent variable */
depvar = y,
                                    /* endogenous variable */
endog = x,
                                   /* instrumental variable */
inst = z,
                                    /* exogenous variable */
exog = ,
                                    /* variables defining absorbed fixed effects */
fe = i c t,
                                    /* incremental on iteration number */
FE iter = 1,
                                    /* variable defining cluster level */
cluster = c,
                                    /* other variables to be carried along to final dataset
othervar = ,
                                    for final analysis */
                                    /* directory for storing temporary data sets */
tempdir = junk,
```

```
regtype = TSLS, /* TSLS or OLS */
showmeans = no, /* yes or no to showing sample summary statistics */
showrf = no, /* yes or no to showing reduced form results of TSLS
model */
showols = no, /* yes or no to OLS without cluster correction */
dosurveyreg = no, /* yes or no to doing PROC SURVEYREG */
wide = no, /* yes or no to wide format table */
estresult = out_data /* data set for outputting estimates */
);
```